

Perform
RNA-Seq
Experiment

Find Genes
and
Functions
that Change
in Your Data

Discover
Regulatory
Motifs

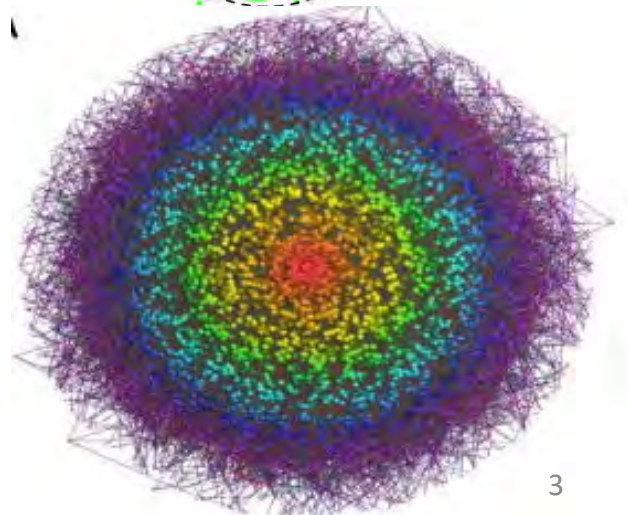
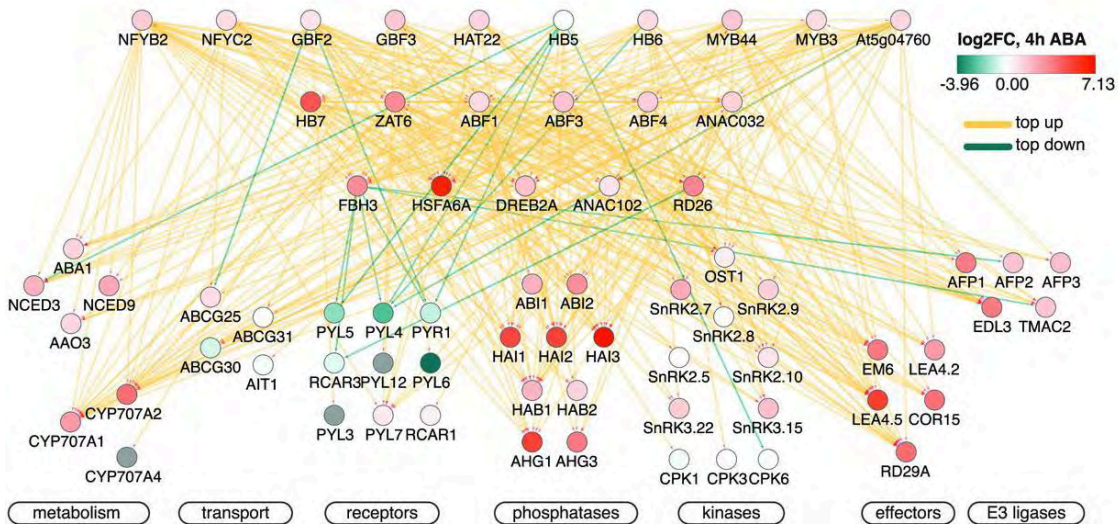
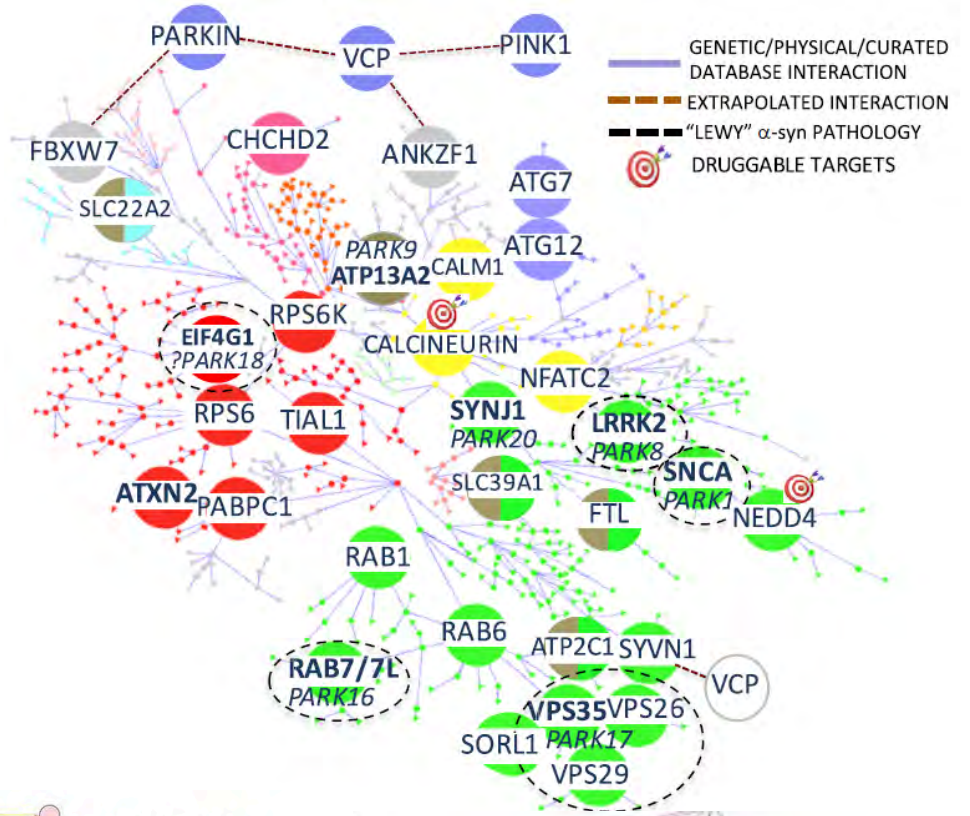
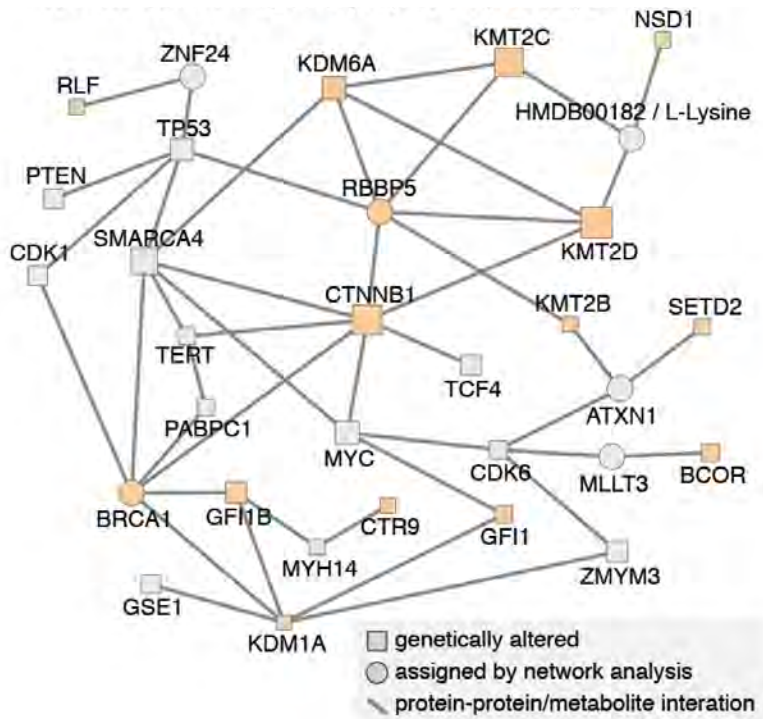
Learn How
to Compare
Data

Understand
Big Data
Approaches

Identify
Disease
Networks

Learning Objectives

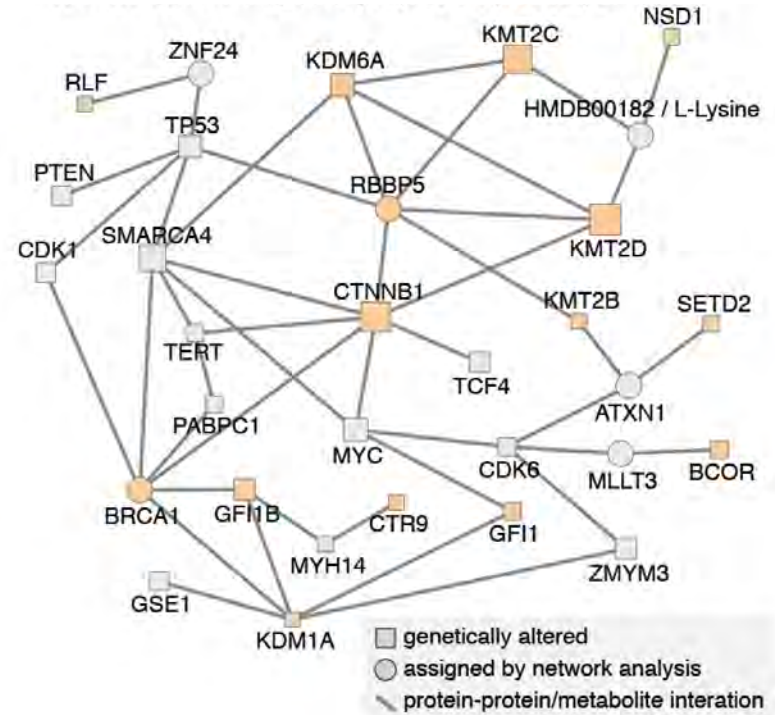
- Know how to represent biological data using graph theory
- Know how to describe a graph (network) using an adjacency matrix
- Understand methods for finding network modules
- Understand how networks integrate data



Network Models

In Today's Lecture:

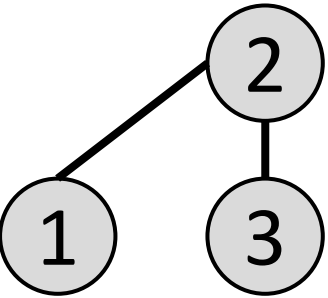
- Structure of network
 - Nodes: molecules
 - Edges: relationships
 - Physical
 - Genetic
 - Statistical



Graph Terminology

- $G=(V,E)$
- Undirected vs. directed
- Weights – numbers assigned to each edge
- Degree(v) – number of edges incident on v
 - In-degree and out-degree
- Path from a to b is a series of vertices $\langle a, v_0, \dots, b \rangle$
where edges exist between sequential vertices.
- Path length = sum of edges weights
(or number of edges) on path.

Adjacency Matrix



$a_{ij} = 1$ if there is an edge between i and j
 0 otherwise

Let $B = A^N$: $b_{ij} = m$ iff there exist exactly m paths of length N between i and j .

	1	2	3
1	0	1	0
2	1	0	1
3	0	1	0

\times

	1	2	3
1	0	1	0
2	1	0	1
3	0	1	0

$=$

	1	2	3
1	1	0	1
2	0	2	0
3	1	0	1

Shortest Path Algorithms

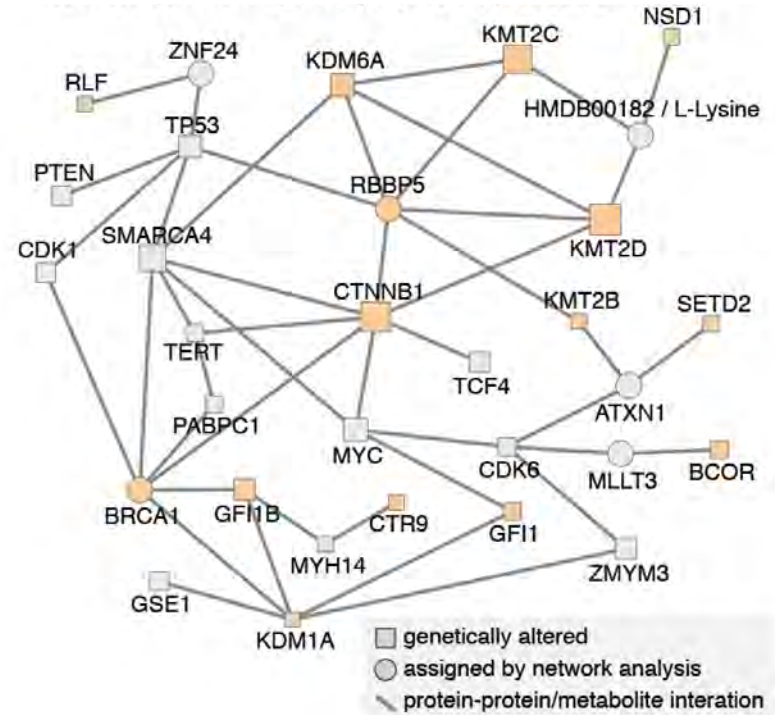
- Efficient Algorithms for
 - single pair (u,v)
 - single source/destination to all other nodes
 - all-pairs

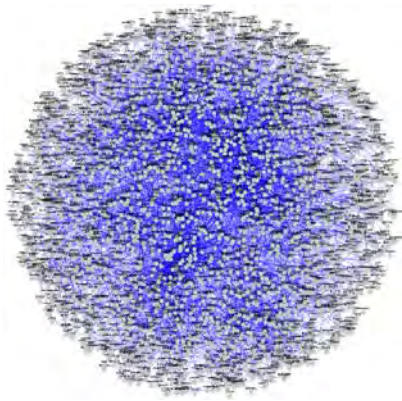
Good place to learn more:
“Introduction to Algorithms”
by Cormen, Leiserson, Rivest, and Stein.

Finding Modules

In Today's Lecture:

- Use the network to organize and simplify the relationships
 - Predicting Function of Genes
 - Identifying Proteins Families, Co-regulated genes
 - Integrating Data

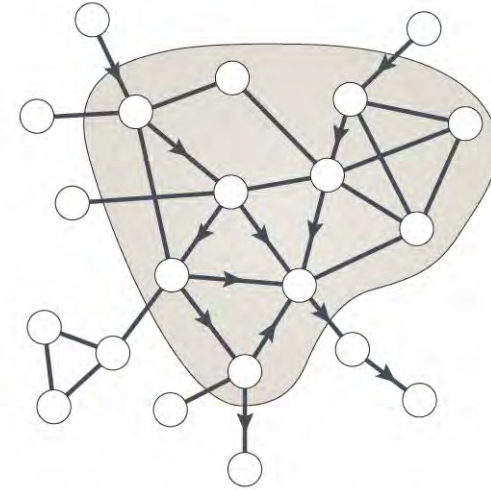




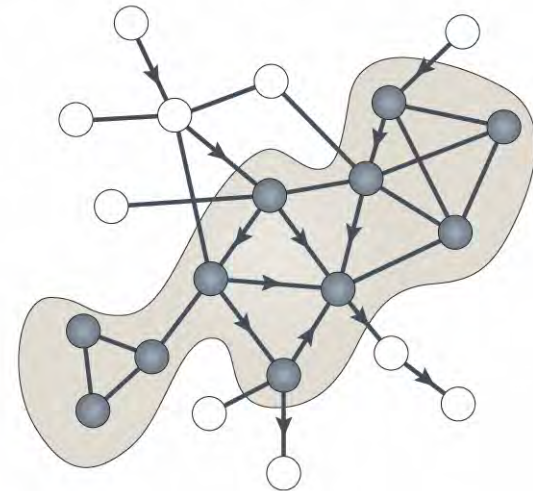
Finding Modules

- **Topological module:**
 - locally dense
 - more connections among nodes in module than with nodes outside module
- **Functional module:**
 - high density of functionally related nodes

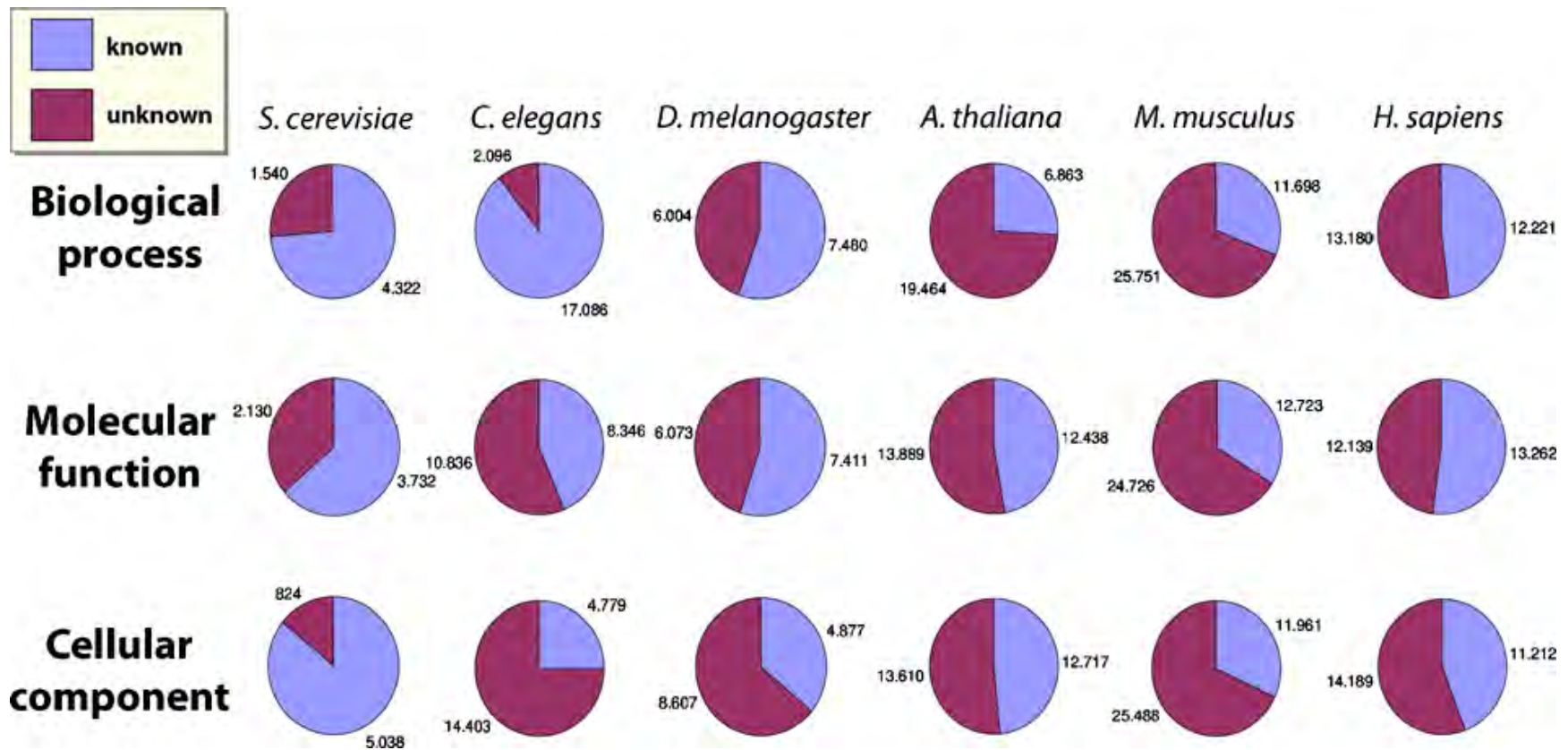
a Topological module



b Functional module



Can we use networks to predict function

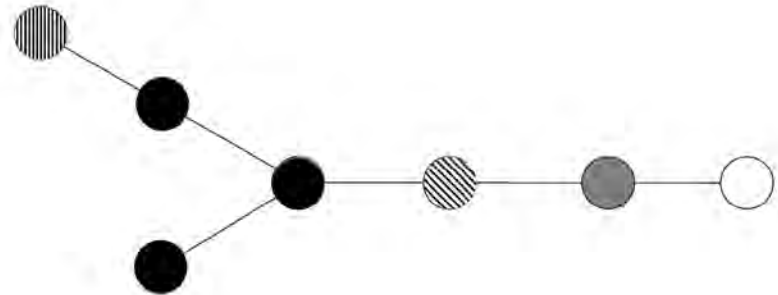
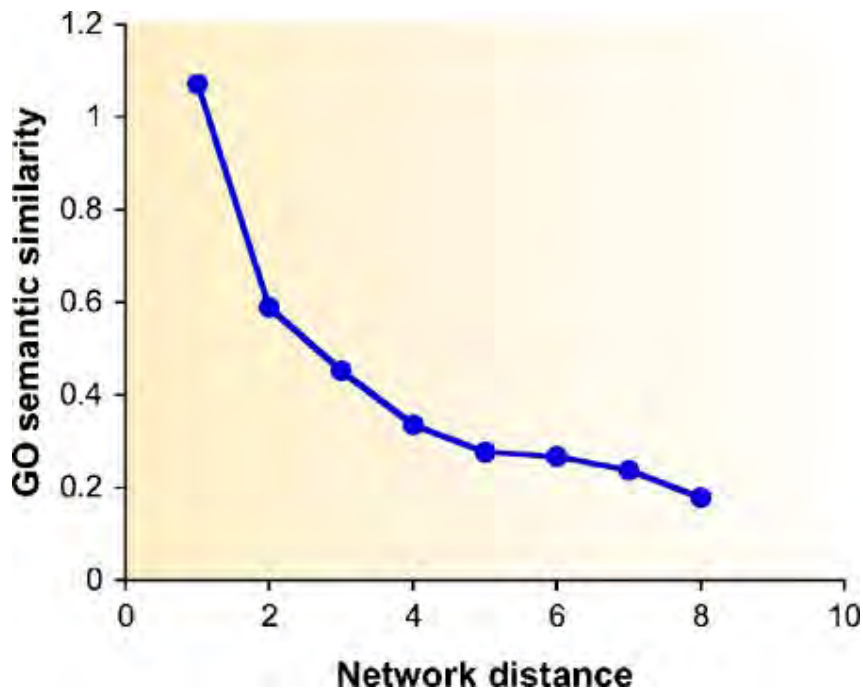


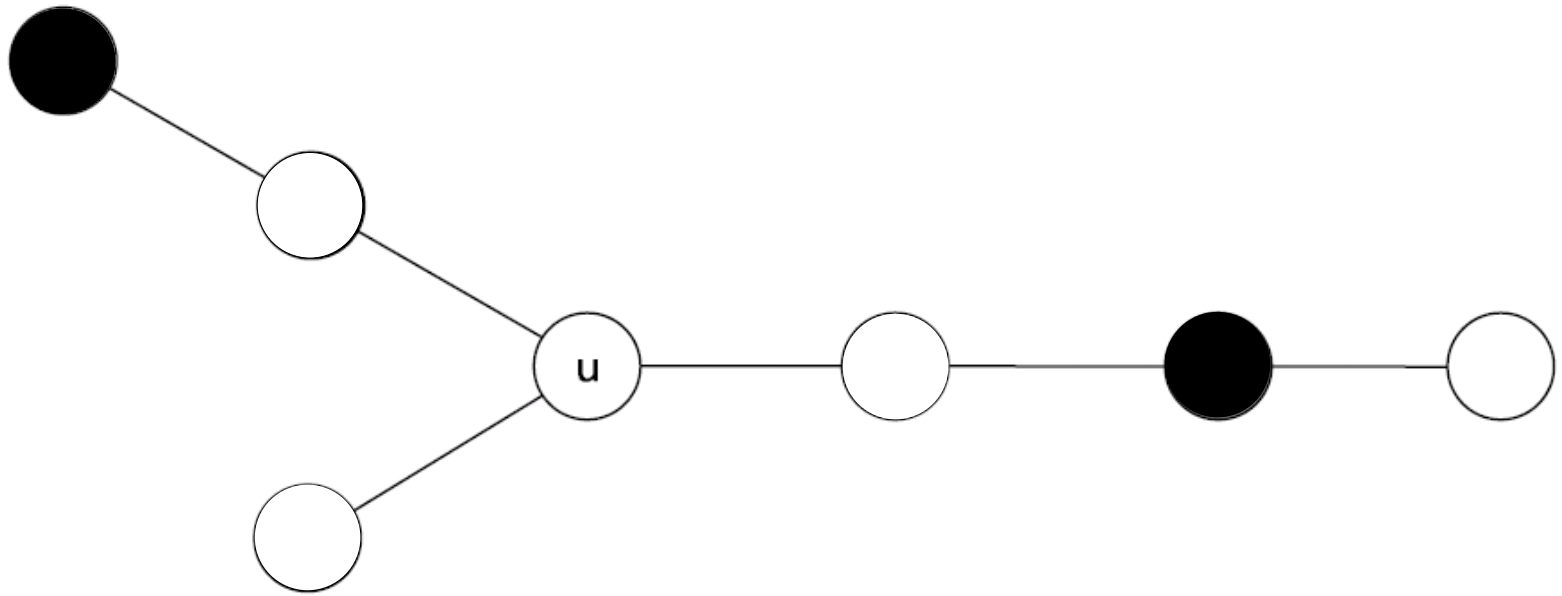
Network-based prediction of protein function

Roded Sharan, Igor Ulitsky & Ron Shamir

doi:10.1038/msb4100129

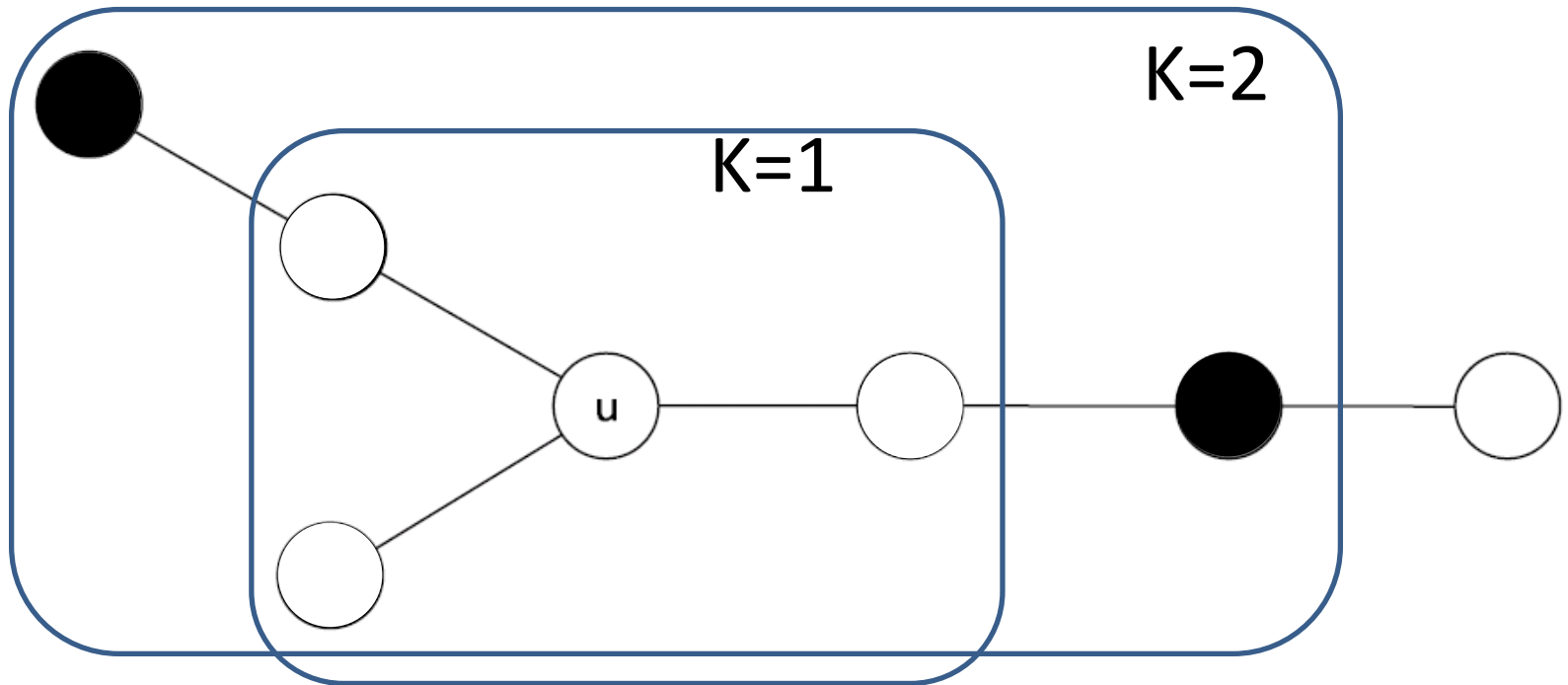
Can we use networks to predict function?





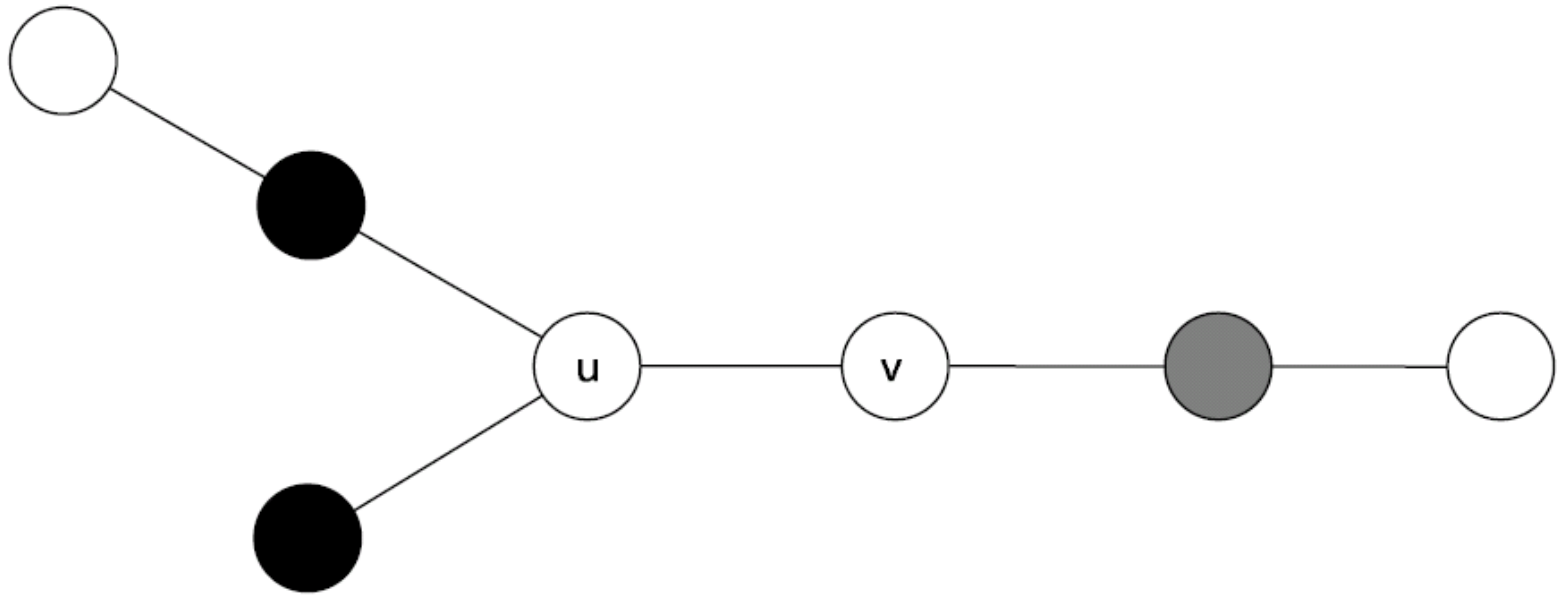
Goal:

Systematically deduce the annotation of unknown nodes u from the known (filled) nodes



“Direct” method for gene annotation

- K-nearest neighbors
 - assume that a node has the same function as its neighbors

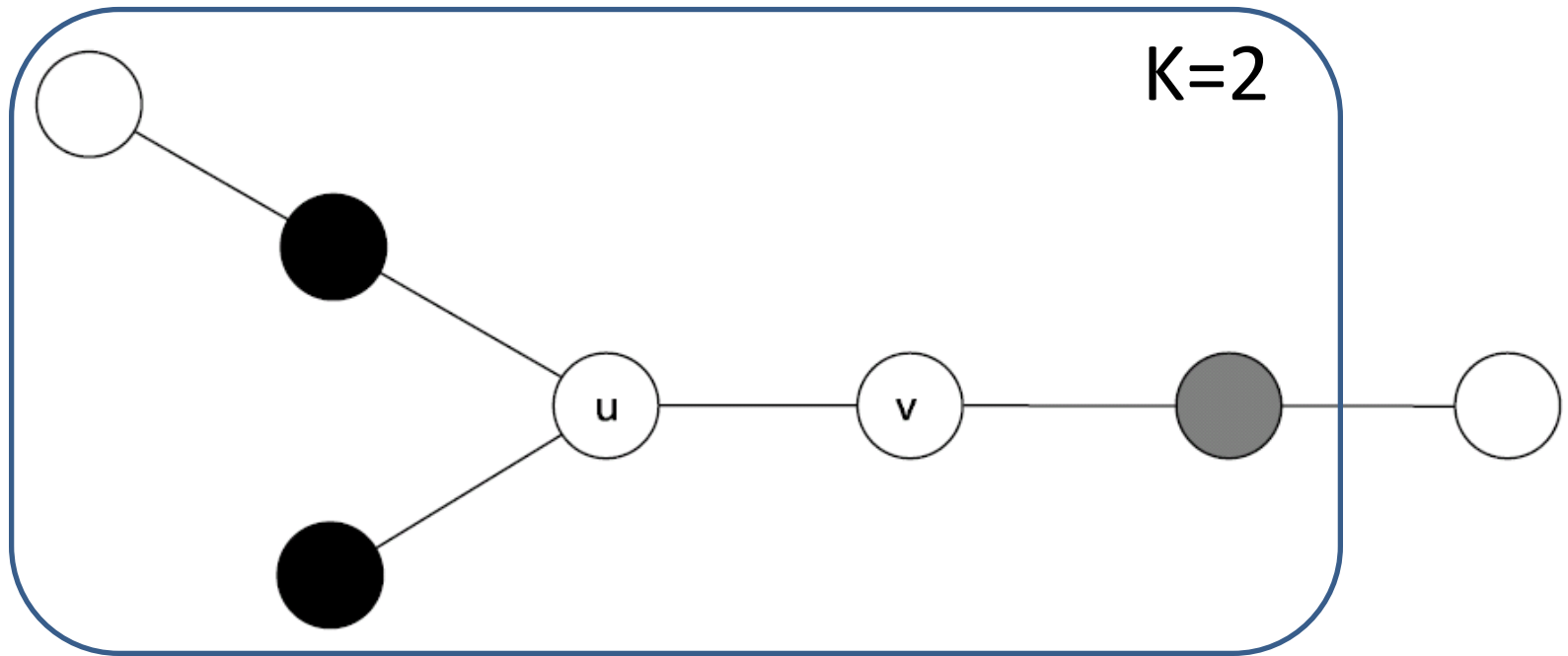


Advantages of kNN approach:

very easy to compute

Disadvantages:

how do you choose the best annotation?



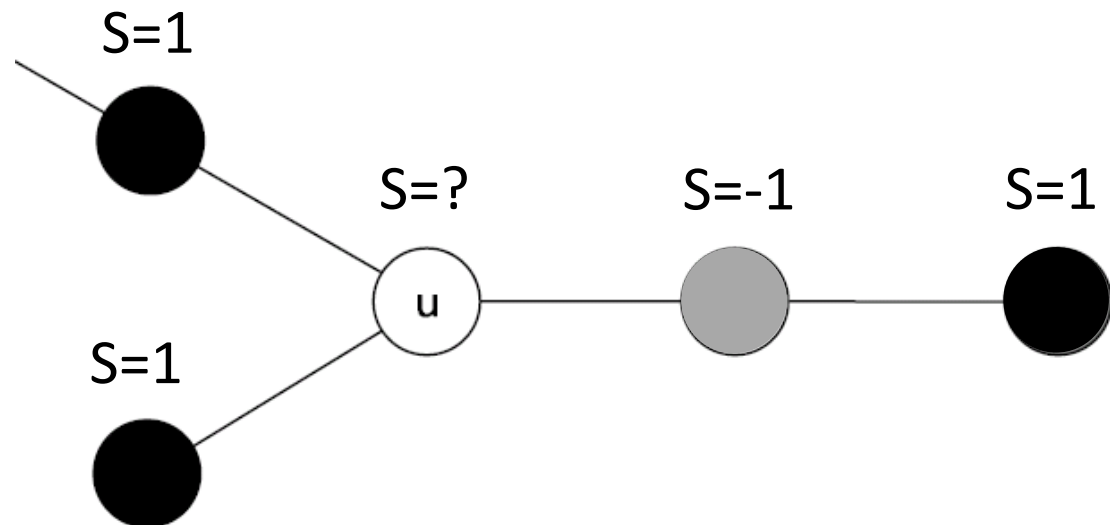
Should u and v have the same annotation?

A two-nearest neighbor approach would say yes.

But u seems more likely to be black and v more likely to be grey.

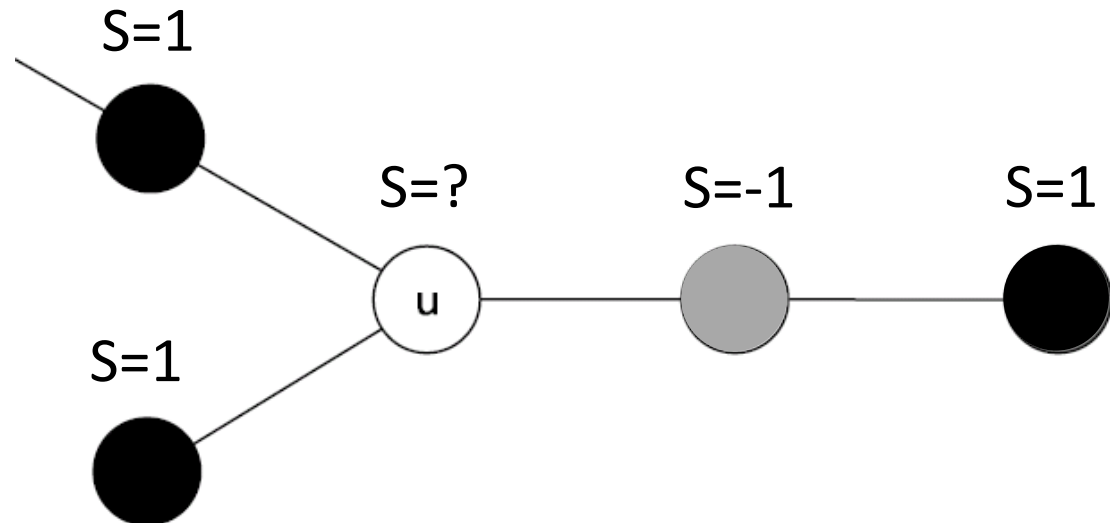
An algorithm for annotation

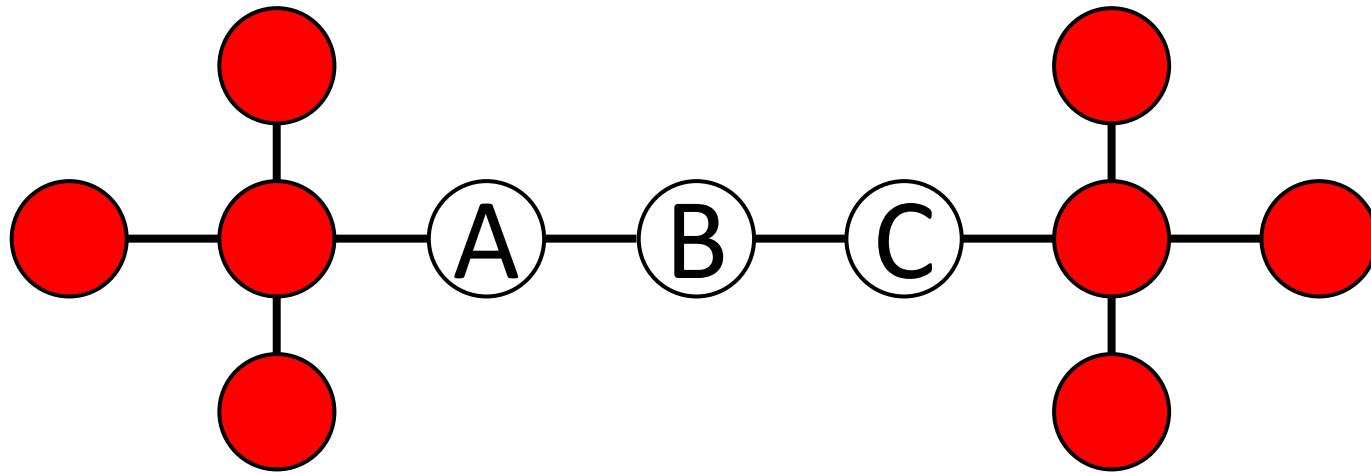
- Motivation: maximize agreement in annotation among connected nodes



An algorithm for annotation

- For each annotation:
 - $S_v = +1$ if v has the annotation, -1 otherwise
 - Procedure: for each unassigned node u , set S_u to maximize $\sum S_u S_v$ for all edges (u,v)
 - iterate until convergence



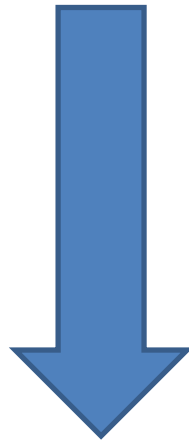
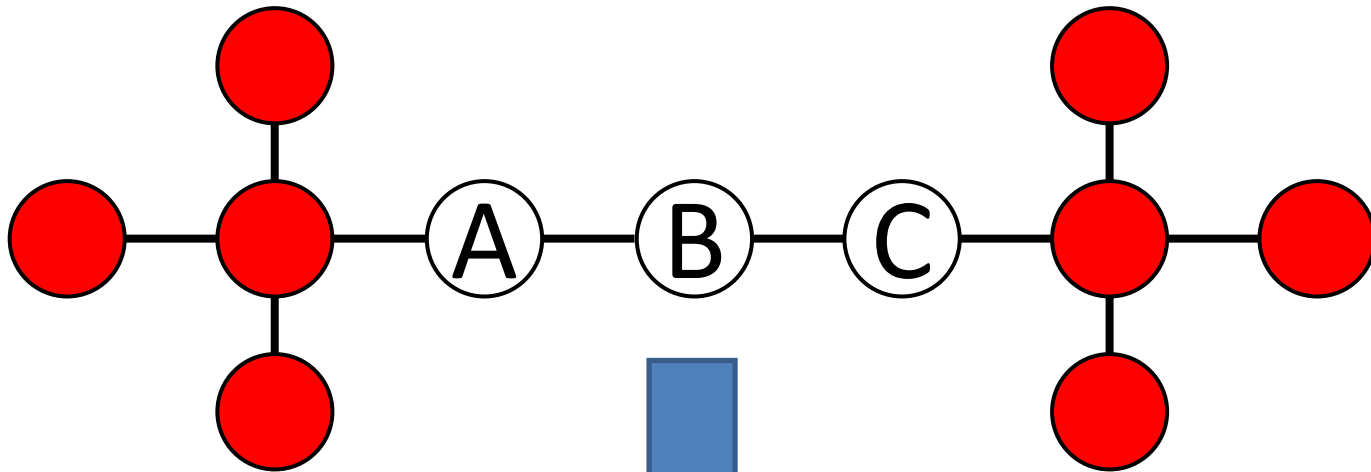


Local search may not find some good solutions.

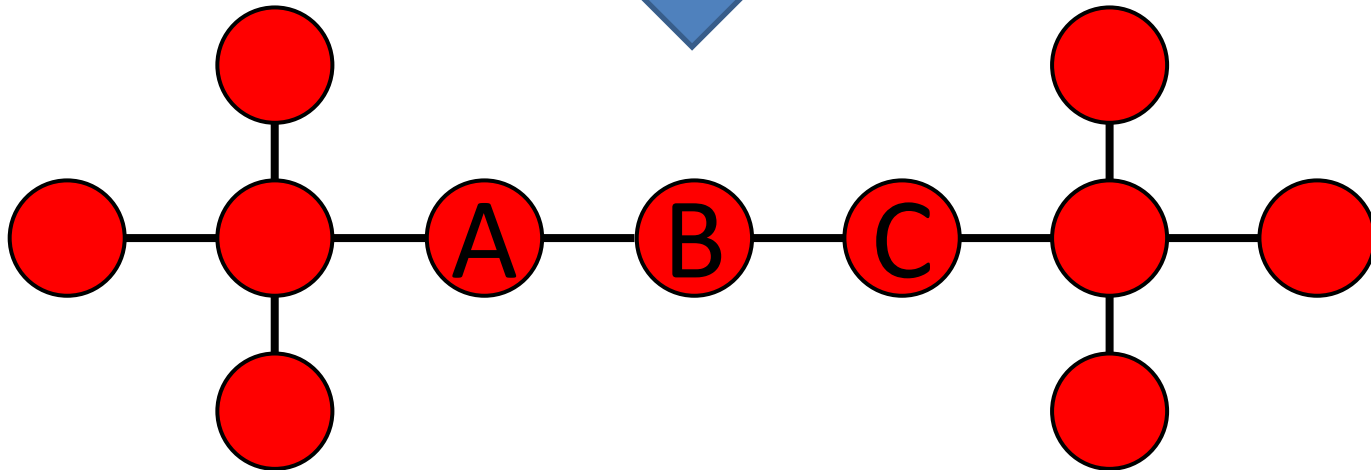
$\sum S_u S_v$ does not improve if I only change A or C. Changing only B makes the score worse.

$S_v=1$ if v has the annotation, -1 otherwise

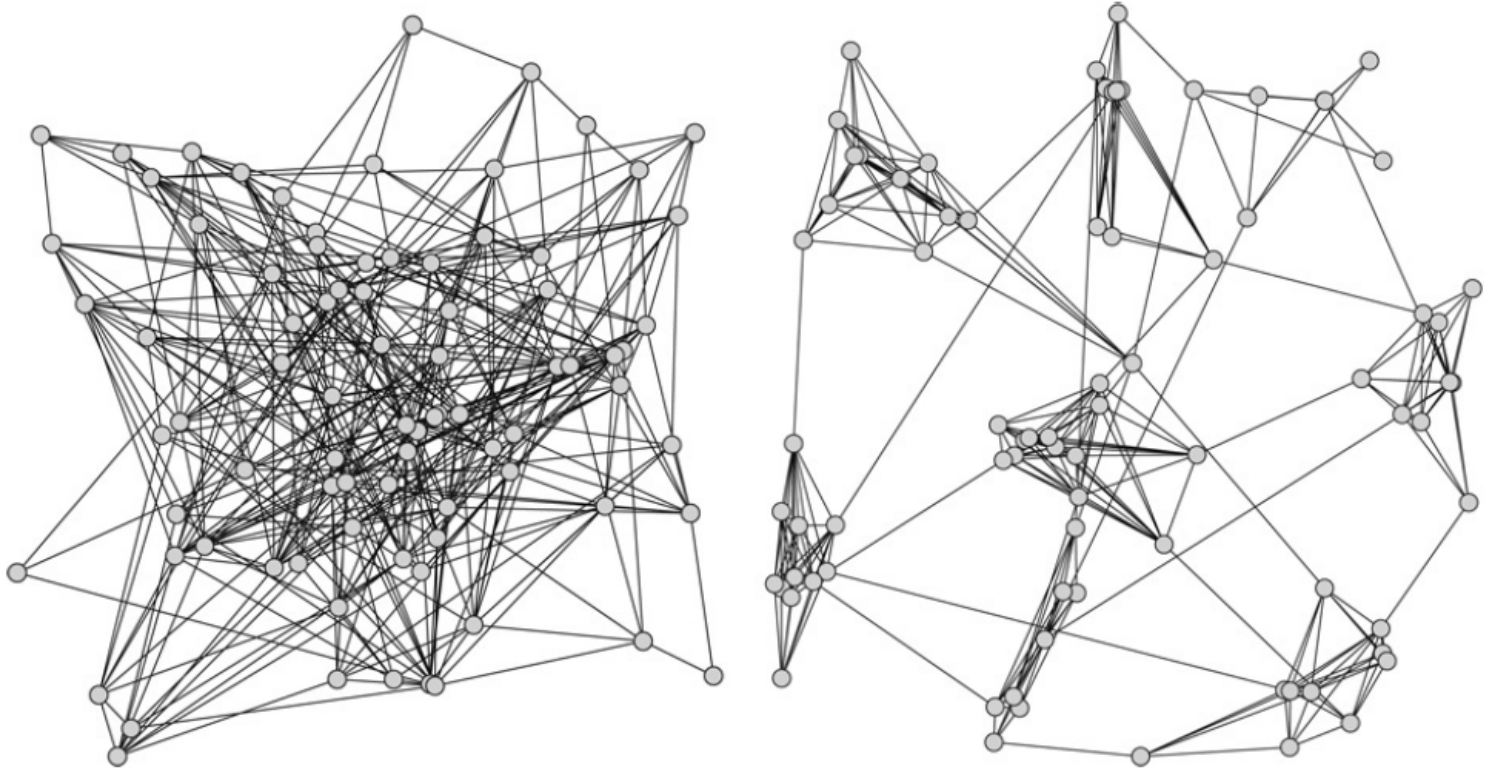
Goal: maximize $\sum S_u S_v$ for all edges (u,v)



Can't get there
by a local optimization



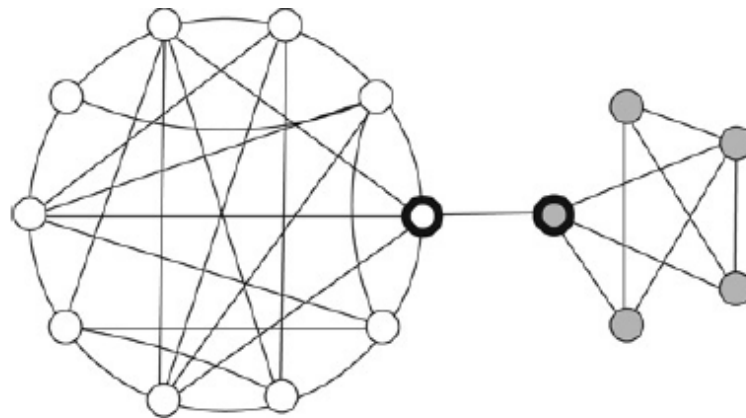
Clustering Graphs



Goal: divide the graph into subgraphs each of which has lots of internal connections and few connections to the rest of the graph

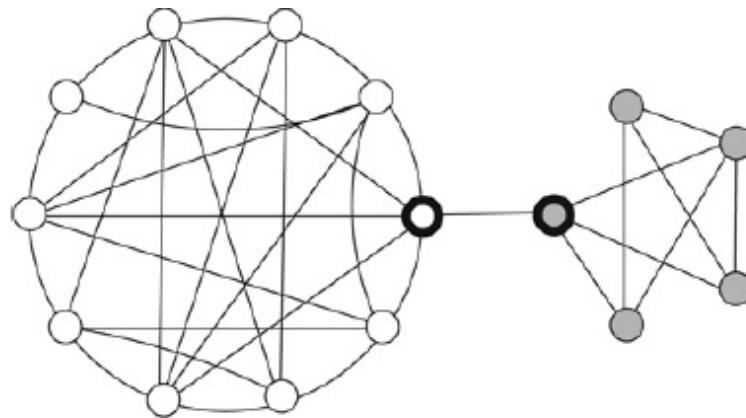
Betweenness clustering

- Edge betweenness = number (or summed weight) of shortest paths between all pairs of vertices that pass through the edge.
 - Take a weighted average if there are >1 shortest paths for the same pair of nodes.



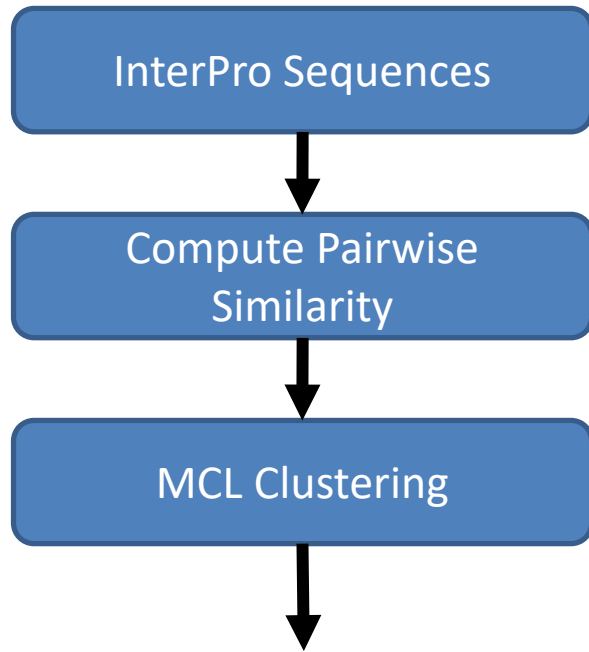
Betweenness clustering

- Repeat until $\max(\text{betweenness}) < \text{threshold}$:
 - Compute betweenness
 - Remove edge with highest betweenness

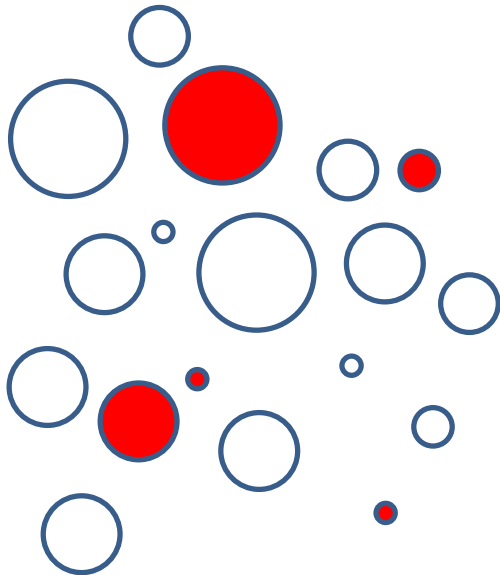


Example

- Identifying protein families
- BLAST will identify proteins with shared domains, but these might not be very similar otherwise (eg: SH2, SH3 domains)



InterPro ID	No. of families	Domain description
IPR001064	141	Crystallin
IPR000504	110	RNA-binding region RNP-1 (RNA recognition motif)
IPR003006	107	Immunoglobulin and major histocompatibility complex domain
IPR000531	97	TonB-dependent receptor protein
IPR003015	96	Myc-type, helix-loop-helix dimerisation domain
IPR001680	76	G-protein β WD-40 repeats
IPR000561	73	EGF-like domain
IPR000169	72	Eukaryotic thiol (cysteine) proteases active sites
IPR001777	42	Fibronectin type III domain

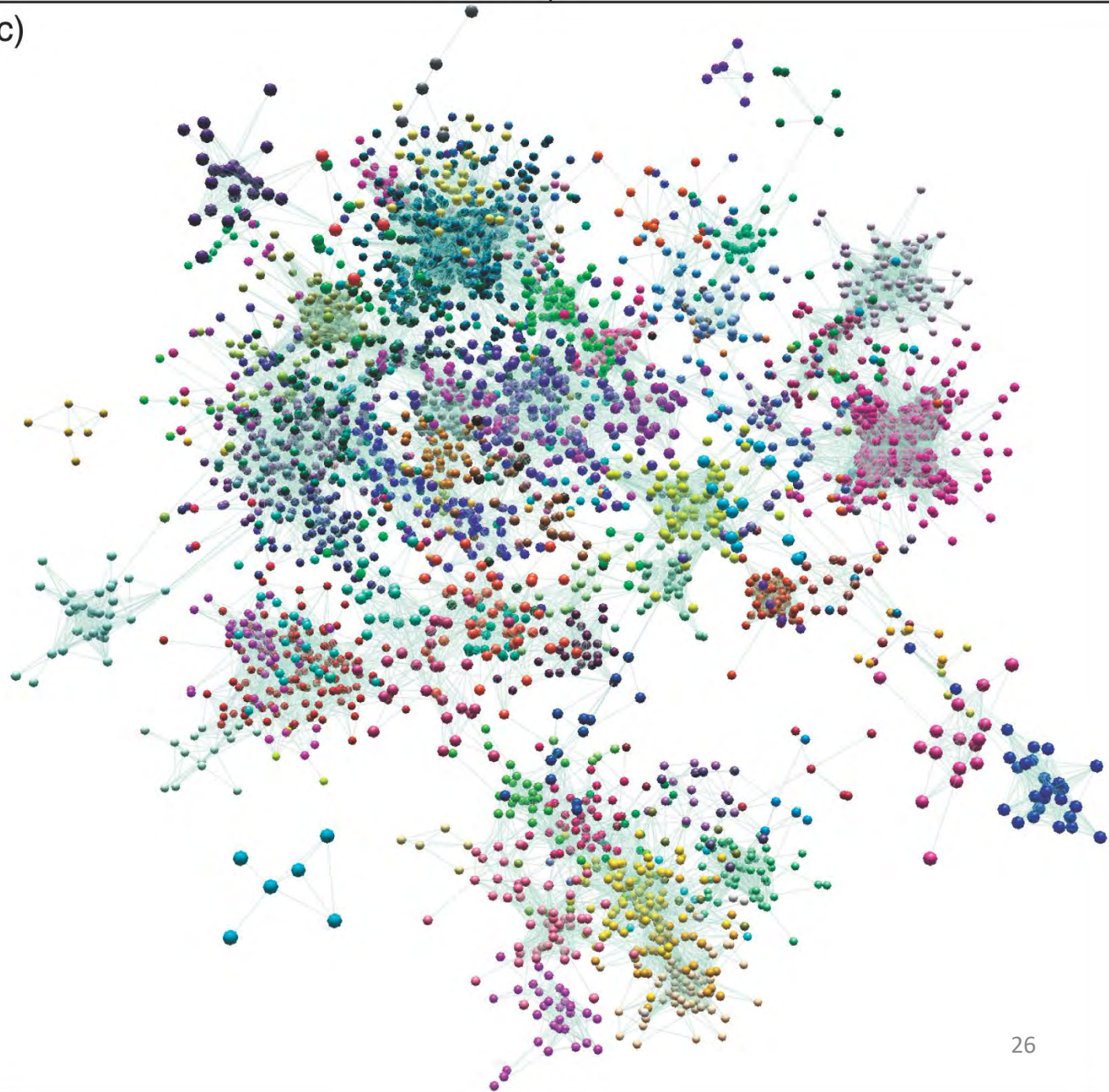


Distinct clusters identified by MCL can still share a common domain

Example

- Clustering expression data for 61 mouse tissues
- Nodes = genes
- Edges = Pearson correlation coefficient $>$ threshold
- Network gives an overview of connections not obvious from hierarchical clustering

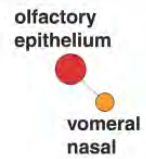
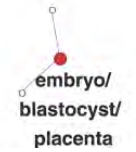
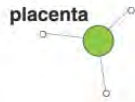
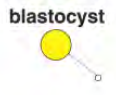
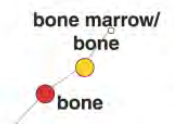
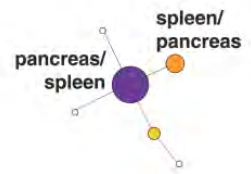
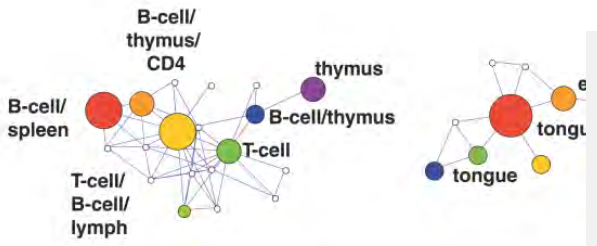
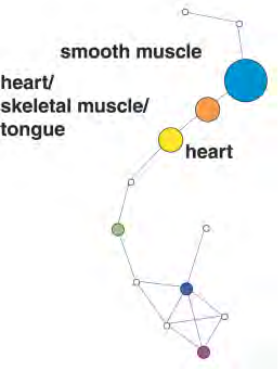
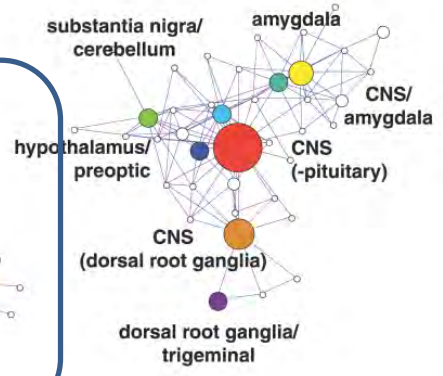
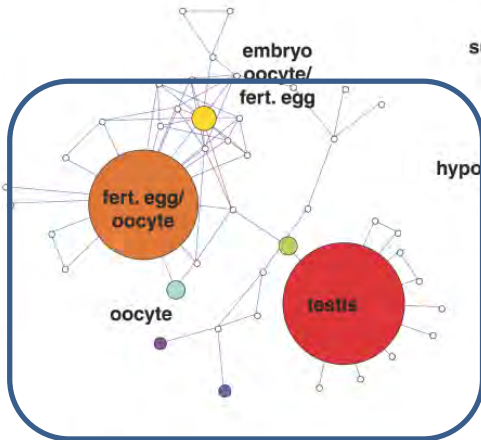
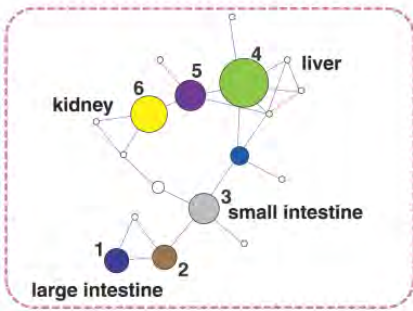
c)



Nodes=genes
Edges=pearson
correlation of
expression in
mouse tissues
Clustered by
MCL

Freeman, *et al.*(2007) PLoS
Comput Biol
3(10): e206.
doi:10.1371/journal.pcbi.0030206

c)



Cluster 4 = liver specific
 Cluster 6 = kidney specific
 Cluster 5 = both liver and kidney

Largest clusters are gamete-specific