Lecture Slides for Tuesday March 31st

11:05 AM EDT by Zoom

https://mit.zoom.us/j/348659452

For audio you can use your computer or call:

US: +1 646 558 8656 or +1 669 900 6833

Meeting ID: 348 659 452

International Numbers:

https://mit.zoom.us/u/adLEbsadSS

Note: class will be recorded and posted for later viewing.

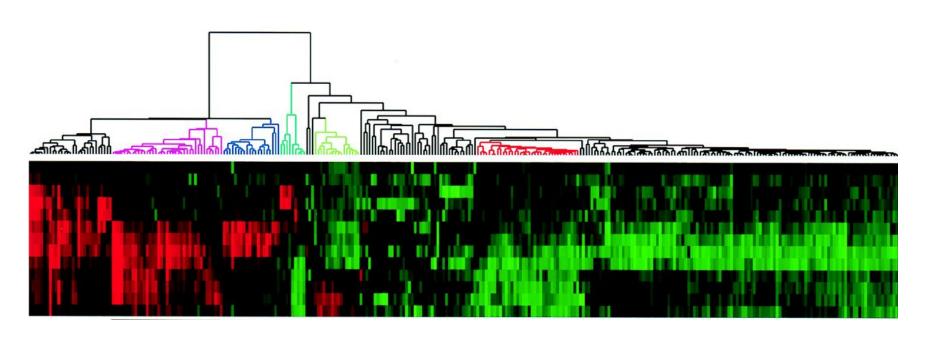
My Revised Lecture Schedule

Date	Topic
March 31st	Cluster, PCA
April 2 nd	RNA-Seq
April 7 th	Transcriptional Regulation

Learning Objectives

- Manually cluster small vectors using k-means clustering
- Describe the results of Principal Component Analysis (PCA)

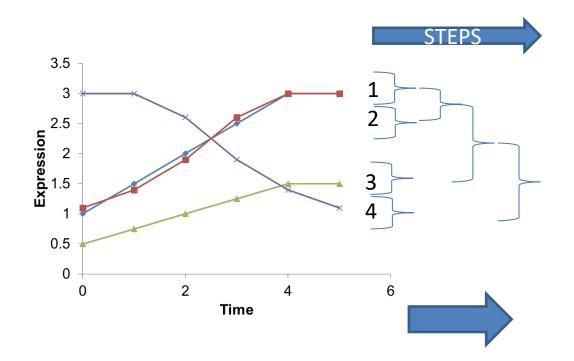
Lightning Review of Hierarchical Clustering



Two types of approaches: Agglomerative & Divisive

Agglomerative:

- Initialize: Each vector is in its own cluster
- Repeat until there is only one cluster:
 - Merge the two most similar clusters.



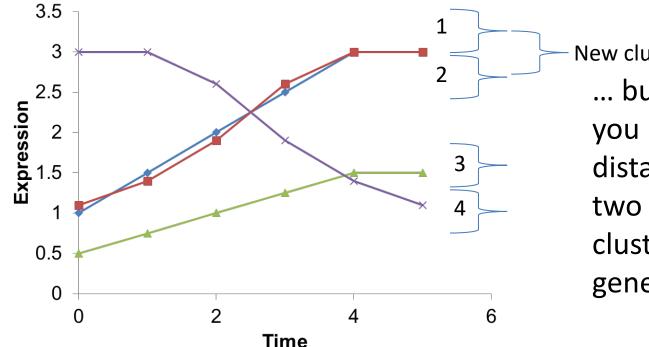
Step 1: each gene is its own cluster

Step 2: combine the two most similar genes

Step 3: find the two most similar clusters

Several options:

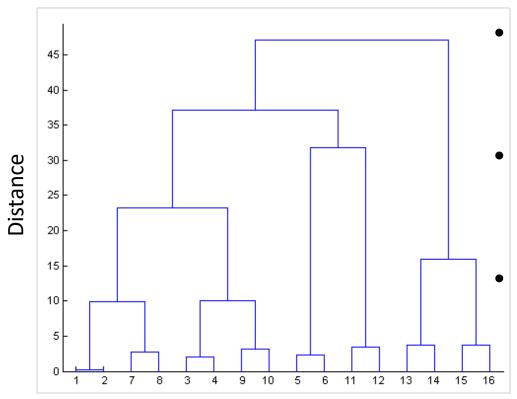
minimum distance between members of cluster A,B maximum distance between members of cluster A,B average distance between members of cluster A,B



New cluster

... but I have not told you how to compute distance between the two genes in the new cluster with individual genes

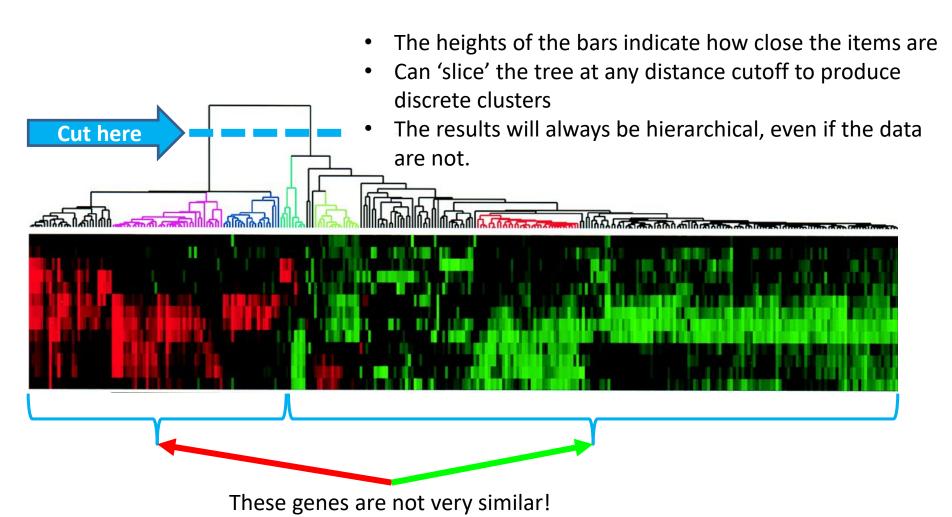
Dendrograms



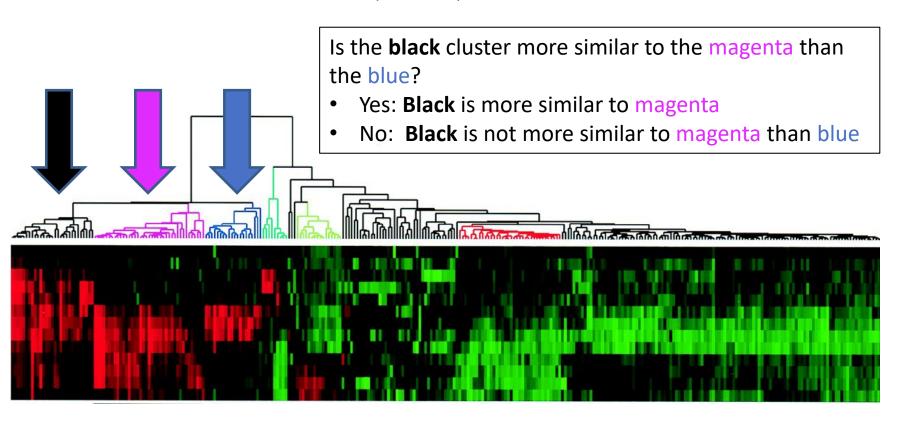
Data items (genes, etc.)

- The final cluster is the root and each data item is a leaf
- The heights of the bars indicate how close the items are
 - Can 'slice' the tree at any distance cutoff to produce discrete clusters
 - The results will always be hierarchical, even if the data are not.
 - The order of the leaf nodes is not meaningful

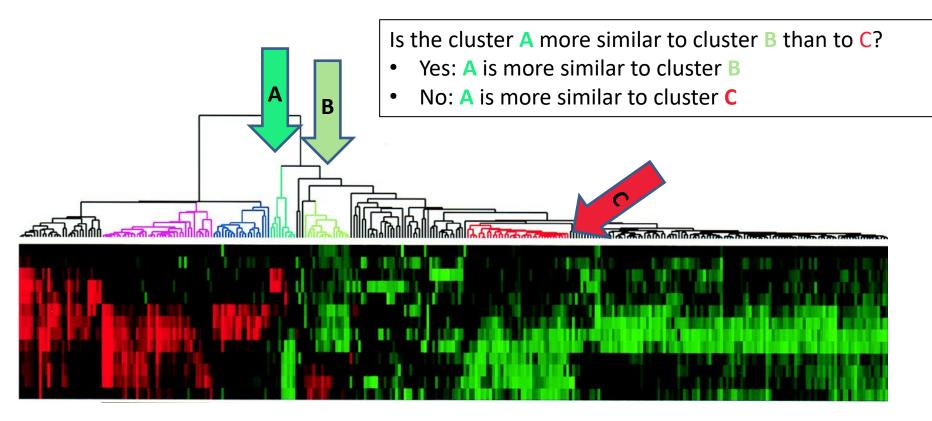
Hierarchical Clustering Links All Samples



Quick Questions



Quick Questions



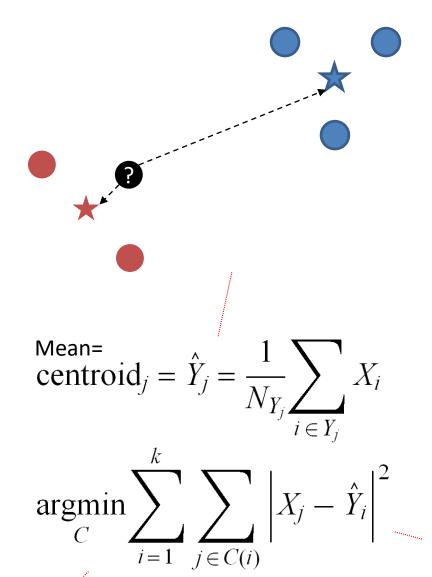
K-means clustering

- Advantage: gives sharp partitions of the data
- Disadvantage: need to specify the number of clusters (K).
- Goal: find a set of k clusters that minimizes the distances of each point in the cluster to the cluster mean:

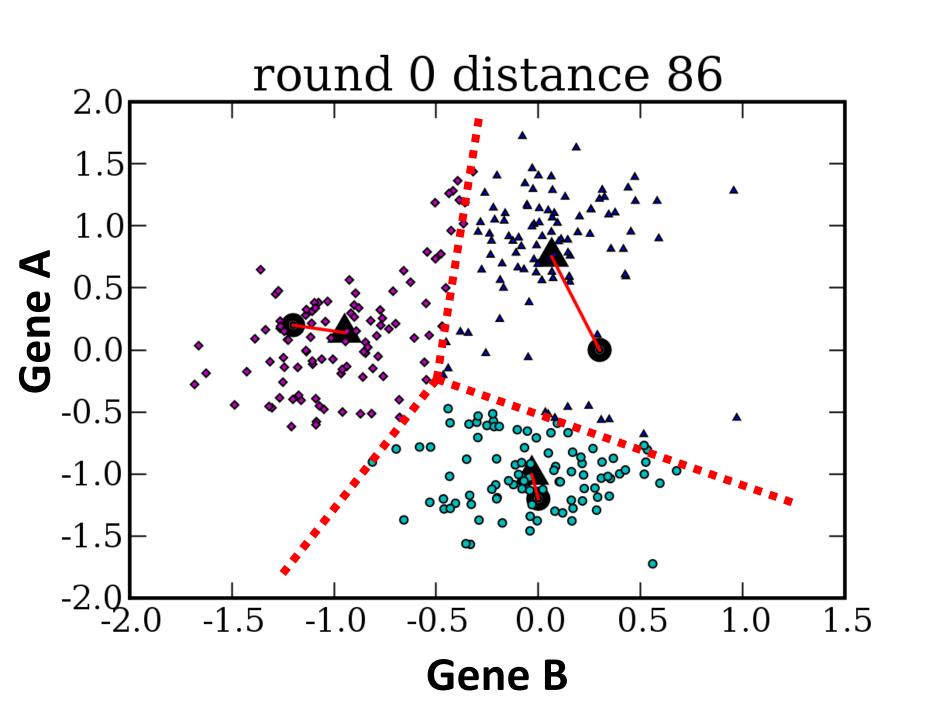
How to cluster with K-means

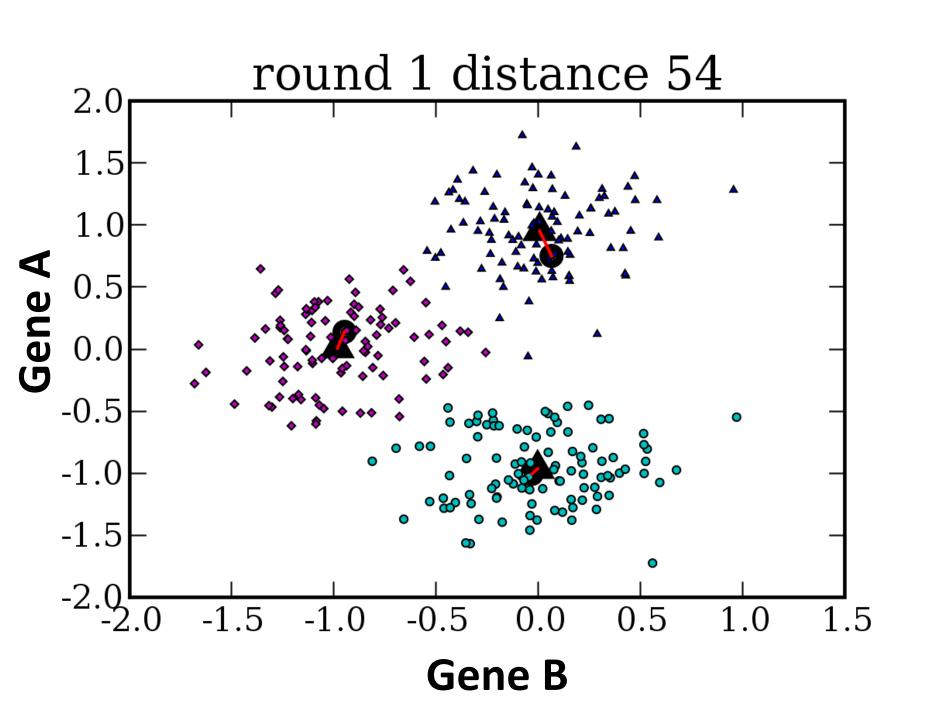
K-means clustering algorithm

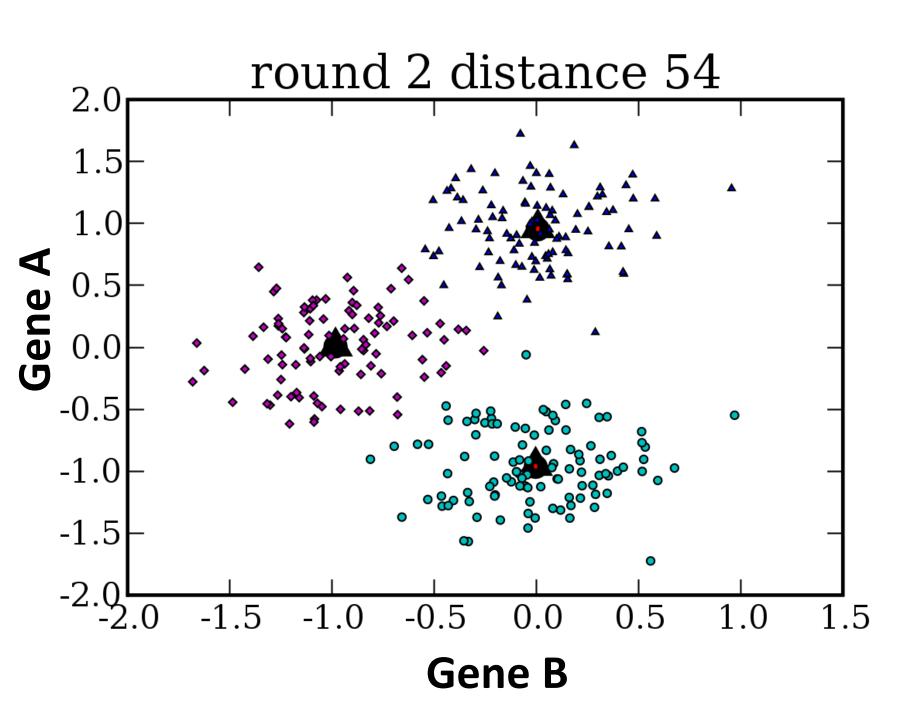
- Initialize: choose k
 points as cluster means
- Repeat until convergence:
 - Assignment: place each point X_i in the cluster with the closest mean.
 - Update: recalculate the mean for each cluster

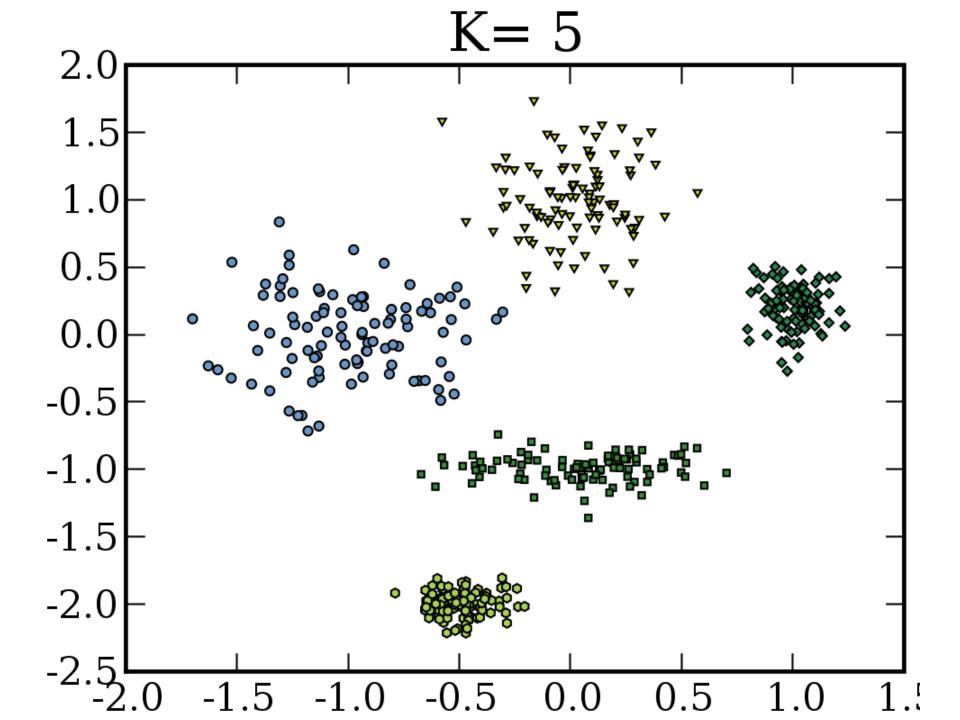


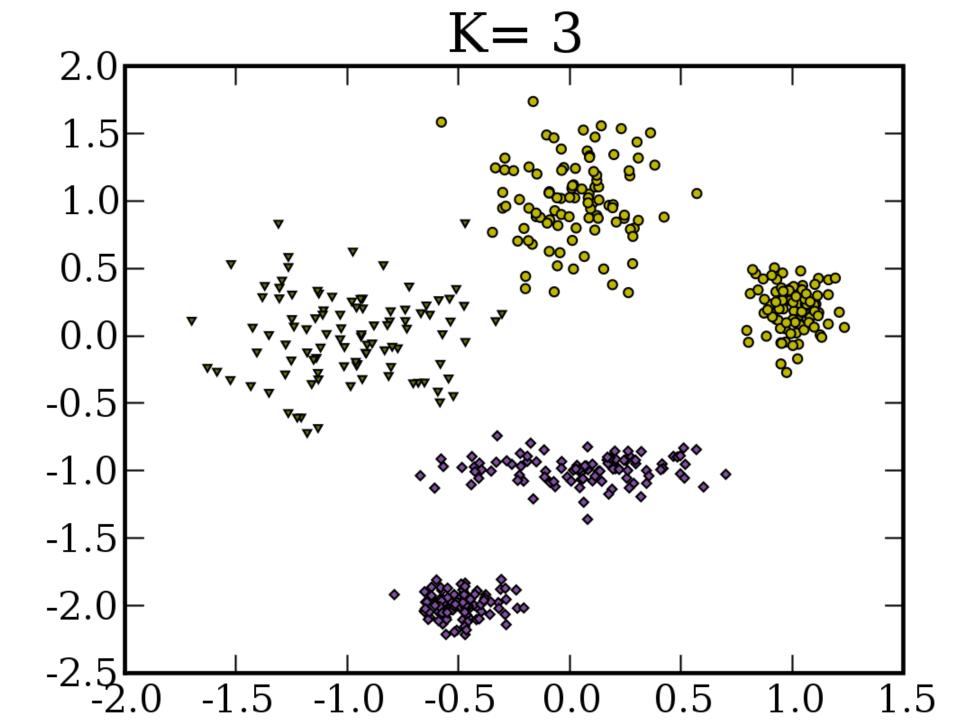


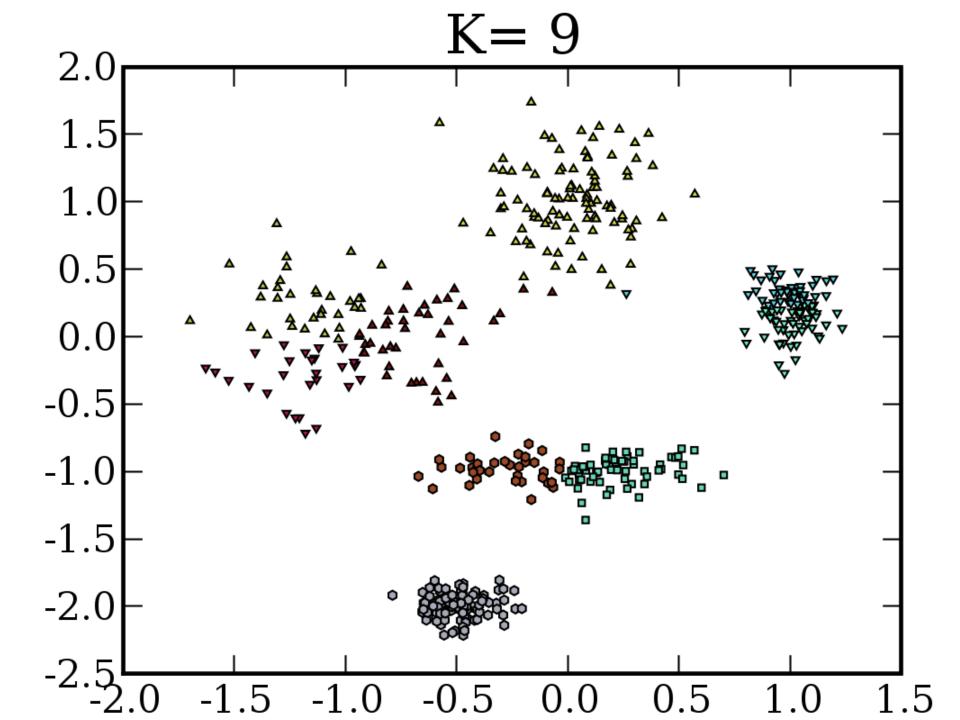




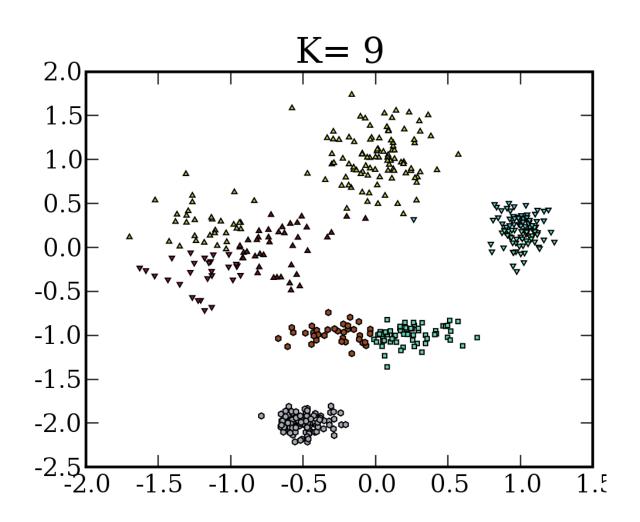


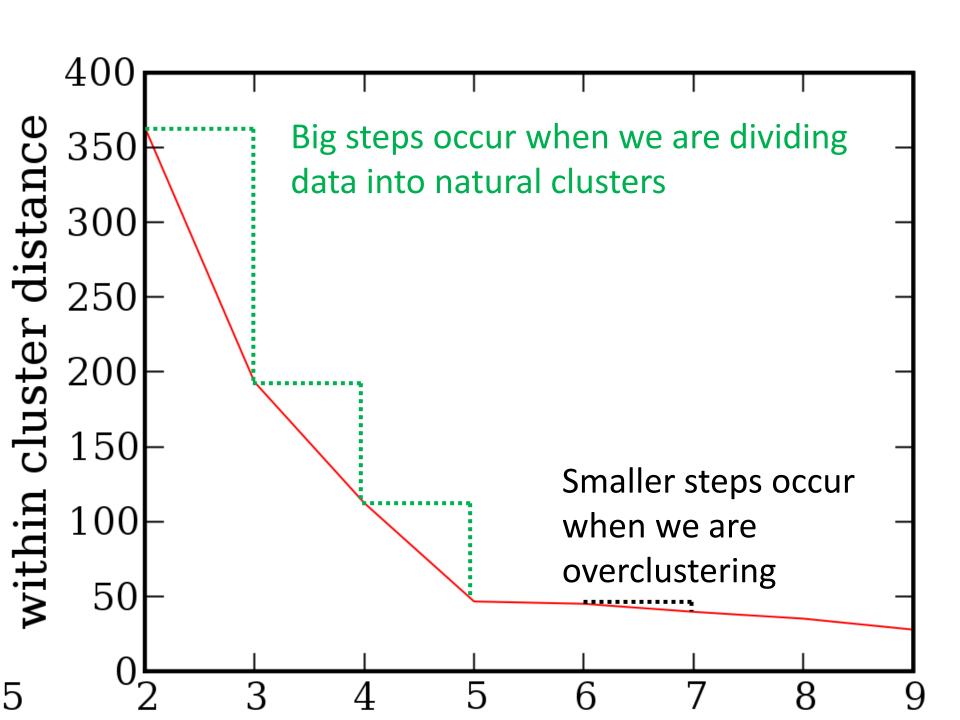




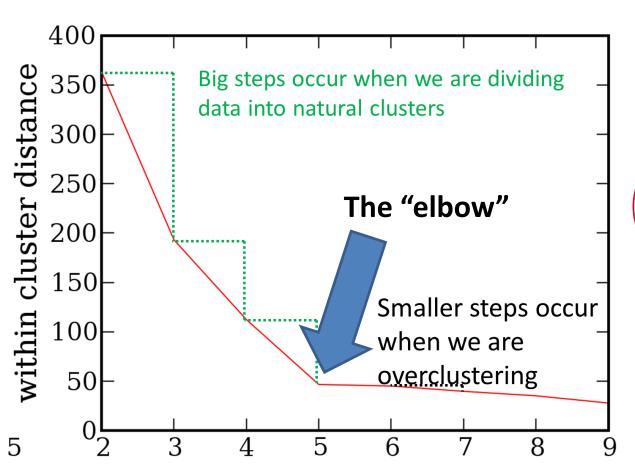


So how do you choose K?





This "elbow" plot can help find the right value of K

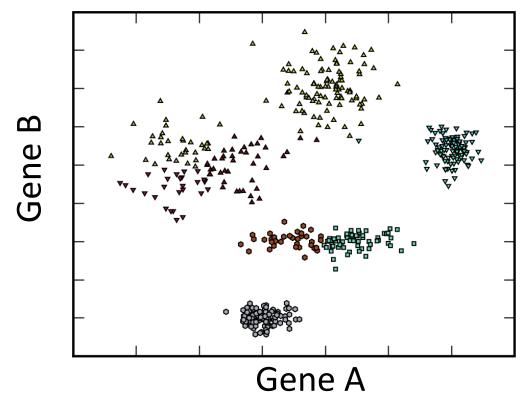




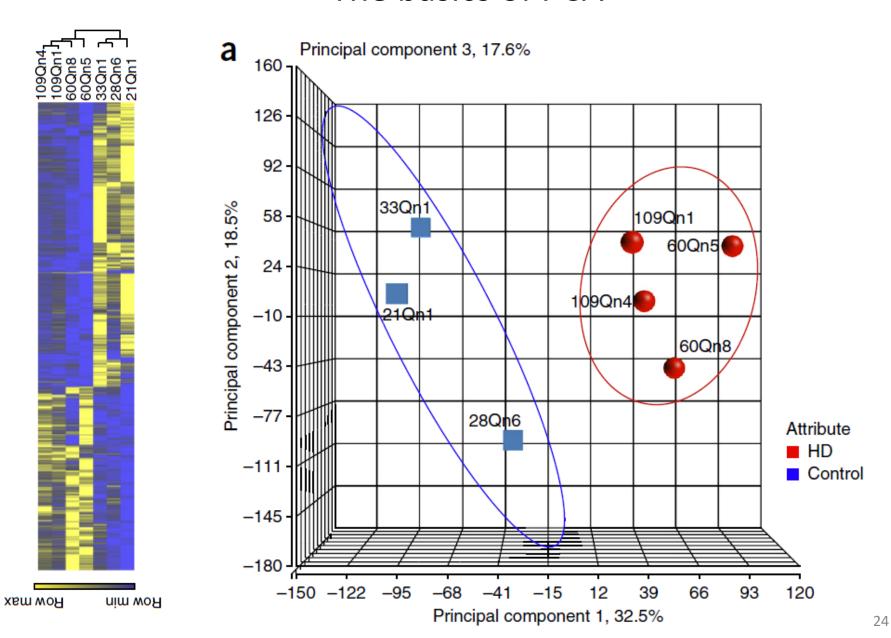
K-means clustering works with vectors of any length, but it's hard to visualize

Dimension =

10 if I cluster genes by their expression in 10 conditions 20,000 if I cluster conditions based on the expression of each gene



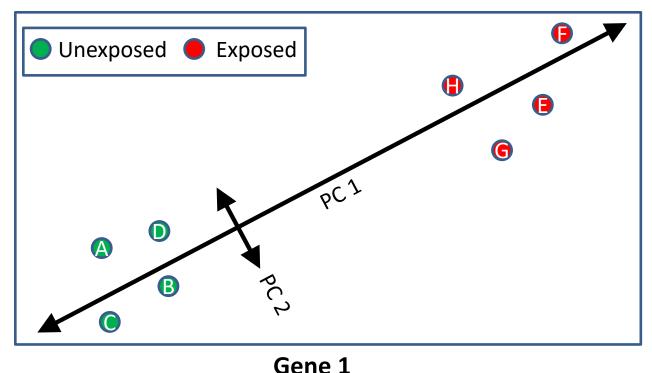
The basics of PCA



Principal Component Analysis

- Each sample is currently described by the expression of roughly 20,000 genes.
- Our goal:
 - to find a 2-D or 3-D way to present the data that captures the greatest variance
 - Obviously, I could select any two genes, but they might be the wrong ones.
 - Can we find "interesting" linear combinations of genes?

Principal Component Analysis



Gene 2

Here's an example where one dimension is almost as good as two.

We can generalize this approach so that one dimension is almost as good as N, where N is large.

- 1. PCA finds useful linear combinations of thousands of variables.
- 2. There are as many PCs as there were dimensions in the original data.
- 3. The PCs are orthogonal.
- 4. Often, a few PCs will capture most of the variance.

